The Low-Energy House Project The Danish Ministry of Energy

FOUNDATIONS FOR ENERGY CONSERVATION HOUSES


## FOUNDATIONS FOR ENERGY CONSERVATION

 HOUSES - a thermal analysis based on examples from five low-energy houses at Hjortekær, DK```
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## PREFACE

The main part of the results in this report was presented at the ENERGEX'82 SESCI Energy Conference at Regina, Saskatchewan, Canada, August 23-29 1982. The material has been reedited and a number of new examples and illustrations has been added.

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In 1978-79 six prototype low-energy houses were built at Hjoxtekær, Denmark. In this report the foundation construction of four slab-on-ground houses and a basement wall are described. The temperature distribution and thus the heat flow through each construction are analysed by means of an orthogonal network computer model for two-dimensional heat flow. In such calculations the thermal conductivity and the actual temperature of the earth are usually uncertain paramw eters. At Hjortekær several temperature sensors were placed in the earth and around the houses as part of the monitoring project, a few for continuous monitoring and the rest for occasional registration。 Thus it has been possible to adjust the input data to bring the calculation model into agreement with the actual conditions.

In the analyses the actual constructions are compared to a corresponding traditional solution. Also, the results from the two-dimensional calculation model are compared to the results from the simplified one-dimensional Danish standard calculation model with respect to heat losses and minimum internal surface temperatures.

The intxoduction of floor heating systems in slab-on-ground houses, especially in energy conservation houses has given the impulse to the second series of analyses where the combination of slab-on-ground constructions and floor heating is analysed as to the varying dimensions of floor insulation and to the introduction of insulated composite foundations.

| Q-DS | Heat flow by Danish standard calculation |
| :--- | :--- |
| Q-1 | Onemdimensional heat flow through floor |
| Q-2 | Two-dimensional heat flow through floor and |
|  | foundation |
| $\Delta Q(2)$ | Difference between $Q-2$ and $Q-1$ |
| rof.l. | Relative floor level (above ground level 0) |
| $t_{e x t}$ | External air temperature |
| $t_{i n t}$ | Internal air temperature |
| $t_{e a r}$ | Constant earth temperature (deep earth) |
| $t_{m i n}$ | Minimum internal surface temperature |
| $t_{f l o}$ | Floor temperature (at embedded tubes) |

## INTRODUCTION

During the recent ten to twenty years most single-family houses in Denmark have been built as one-storey houses without basement, and the main part has been built slab-onground. The foundation is traditionally a weak point, thermally speaking, especially in connection with slab-on-ground constructions. The joining of the walls and the substruc. ture often results in severe thermal bridges. It is a comm mon winter observation that the snow close to a house melts away very quickly even at the noxth wall.

Cold bridges in the foundation construction increase the transmission heat loss and should be minimized or avoided in energy conservation houses if only for that reason. They also lower the surface temperature at the base of the wall and the adjacent floor and thus cause discomfort as well as condensation risk. Condensation to a small extent may only bring about maintenance problems, but in severe cases the result may be mould or (in timber structures) dry rot.

Another problem may often occux in energy conservation houses. To increase the efficiency of heat pumps or active solar systems a low-temperature heating system is preferred, mostly floor heating. The combination of a floor heating system and a slab-on-ground construction introduces new demands to the floor insulation as well as to the foundation construction.

In 1978-79 six detached singlewfamily energy conservation houses were built at Hjorteker, north of copenhagen, as part of the Danish Energy Research and Development programme, [1]. The six prototypes are all different as to architectural design, choice of building materials, heating systems etc, and they offer a diversity of technical solutions to the problems of thermal bridges, [2]. All six houses have a living area of about $120 \mathrm{~m}^{2}$, five of them in one storey and the sixth in two storeys (and a basement) one of the onestorey houses has a crawl space and is not included in this investigation, and the remaining four are slab-on-ground houses. One of the slab-onoground houses (E) has a basement under the central section of the house, figure 1 .
$\left.\begin{array}{|l|cccccc|}\hline \text { House } & A & B & C & D & E & F \\ \hline \text { Number of storeys } & & 1 & 1 & 1 & 1 & 1\end{array}\right]$

Figure 1. The six low-energy houses at Hjorteker - Type description.

Figure 2 (left) shows a vertical section of the floor and foundation of house $A$. The floor construction consists of single flooring on chocks, 50 mm of mineral wool, vapoux barrier (polyethylene), concrete slab cast on site, 50 mm of mineral wool and 200 mm of expanded clay clinkexs. The foundation itself is extremely well insulated, its 225 mm of mineral wool (reaching about 1 m below the ground level) being adjacent to the 200 mm of mineral wool in the wall without any thermal bridge.


Figure 2. Foundations of house $A$.

The inner and outer prefabricated concrete elements rest on 10 annular concreted footings, 0.60 m in diameter, as shown in Figure 3 (and by the dashed line in Figure 2). The working operation is as follows: The reinforced foundation beams are placed on the footings, the bottom is concreted to stabilize the two leaves, a few loose expanded clay clinkers


Figure 3. House A. Annular concreted footings.


Figure 4 .
Commercially developed version of house $A$ foundation.
are put in to level the bottom, and the cavity is insulated with slabs of mineral wool. Only a part of the house has a brick facing - the west and south aspect have a facing of mahogany wainscoting and a more slender foundation insulated
with 100 mm of mineral wool as indicated in figure 2 (right) and in Figure 3 。

This type of foundation construction was put to practical use for the first time in house A at Hjortekær. The con= struction has since been further developed into a U-shaped precast and pre-insulated unit as shown in figure 4 。

Figure 5 shows a vertical section of the floor and foundam tion of house $C$. The house has a concrete floor covered with wall-to-wall coir carpets or tiles. Beneath the conm crete slab ( 100 mm cast on site) there are a vapour barrier, 50 mm of mineral wool, 50 mm of concrete (also cast on site) and 250 mm of expanded clay clinkers. The 50 mm mineral wool is continued vertically as 0.45 m internal foundation insulation. The foundation itself has a concrete base cast on site in an earth trench. On top of this is placed a block of expanded clay concrete, and then another, more slender. The cavity between the expanded clay concrete and the concrete is insulated with 75 mm of mineral wool. It should be noticed that the house has a floor heating system with concreted plastic tubes.


Figure 5.
Foundation of house $C$.

House $D$ has a sandwich foundation built on site, shown in Figure 6. The flooring is parquet or chip boards laid directly on 100 mm rigid mineral wool. From the mineral wool downwards the floor is composed of a vapour barrier, a smoothing (levelling) layer of concrete (approx 40 mm ), about 90 mm concrete cast on site and 200 mm of expanded clay clinkers. In the scullery there is a tile flooring. The foundation base is concreted in an earth trench and the foundation built on top of it from blocks of aerated concrete. A bituminous millboard separates the lightweight concrete from the concrete. The cavity (width 130 mm , depth 600 mm ) is insulated with polyurethane (PUR) foam, sprayed in situe It should be noticed that the aerated concrete below ground level is surfaced (a protective rendering and a special coating)。


Figure 6.
Foundation of house D.

House E has a sandwich foundation as well but of a quite different construction, Figure 7. The floor consists of single flooring, a vapour barrier, 195 mm of reinforced concrete cast on site and 300 mm of mineral wool (the top 80 mm being a very rigid quality) on shingle. The foundation base
and inner leaf were cast on site in form, and the outer leaf was built from blocks of expanded clay concrete the cavity has a depth of 600 mm and is insulated with 125 mm of mineral wool.


Figure 7.
Foundation of house E.

Figure 8 shows a vertical section of the basement floor and the lower part of the basement wall of house F The ground is sloping, and the surface of the basement floor is $1.2 \pi 2.4 \mathrm{~m}$ below ground level (the depth 2.4 m being prevalent) The concrete floor is cast on site on top of 200 mm of mineral wool (on shingle) ofhe basement wall is made of large prefabricated concrete building units as is the rest of the house The composite wall elements in the basement are insulated with 170 mm of mineral wool; the corresponding wall elements above ground level are insulated with 200 mm of mineral wool. Such well insulated concrete building units were used for the first time in house $F$ at Hjortekar. In these new elements the insulation thickness is not reduced at the edges, and the outer and inner leaf are mechanically connected with stainless reinforcement steel only (approx $350 \mathrm{~mm}^{2} / \mathrm{m}^{2}$ ) . Part of the basement has floor
heating installed as shown in Figure 8 , but normally the basement is not heated.


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Figure 8.
Foundation of house F.
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CALCULATION OF TWO-DIMENSIONAL HEAT FLOW

The applied model utilizes the analogy between thermal and electric resistance, [3], and the computer program is an adapted version of an electric resistance program developed at another institute at the Technical University, [4]. Fige ure 9 shows the principle of calculation of the heat flows appearing in the following Figures. The arrows indicate the heat flow through each mesh of the model network (along the chosen surface). The hatched areas indicate the difference between the two-dimensional and the one-dimensional heat flowe The sum of the differences forms the additional heat loss, $\Delta Q(2)$, The illustration suggests that a condition of onemamensjonal heat flow through the floor does exist very often (narrow houses, moderately insulated floors and foundations) it does not. The situation is then as sketched for the wall section.


Figure 9. Jllustration of heat flows.

The total (twomdimensional) heat flow through the floor and the foundation, $Q-2$, is usually given as the onewdimensional ELow through the floor, $Q=1\left[\mathrm{~W} / \mathrm{m}^{2}\right]$, and the above-mentioned addition, $\Delta Q(2) \quad[W$ per running meter foundation along the internal perimeter of the housel. However, $\Delta Q(2)$ in this report is given in $W / m^{2}$ to facilitate the comparison of the different houses. Multiplication by the xwvalue from Figw ure 10 will yield the additional heat flow in $w / m$. We have chosen to include 1.0 m of the wall in all calculations. The distance $x$ depends on the design of the house, the maxjo mum being half the width of the house - if the house is not rectangular $x$ will be smaller. The values used in the anam Iyses are listed in pigure 10 .

| House | A | C | $D$ | $E$ | $F$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $X[m]$ | 3.65 | 2.10 | 2.70 | 2.11 | 2.40 |

Figure 10 . Distance $x$ in the calculation network.

Internal and external temperatures of 21 deg $C$ and 0 deg $C$ respectively have been used for all calculations as has the m almost - constant deep earth temperature 8 deg C. In case of floor heating a uniform floor temperature of 32 deg $C$ at the level of the embedded tubes has been applied. Denmark has approx 70,000 heating degree hours (17 deg c base) in a year, and the average external temperature during the heatm ing season is 3.0 deg $C$. As conservation houses make better use of the free heat and thus have shorter heating seasons the average outdoor temperature 0 deg $C$ has been found appropriate。

Figure 11 shows two examples of heat flow calculations at different internal temperatures and at the design inter* nal/external temperatuxes 20 deg $C /=12$ deg C. The figuxe illustrates how the results in this report within reasonable limits can be used at different thermal conditions. Q-2 can be considered directly proportional to the internal to external temperature difference when only the indoor temperature is varied. With less accuracy $\Delta Q(2)$ can be considered in direct ratio to the same temperature diffexence when only the outdoor temperature is varied The examples indicate that this estimate will be fairly acourate for well insum lated foundations and conservative for moderately insulated foundations at external temperatures below o deg C.

| Example | tint <br> $[\mathrm{C}]$ | $t_{\text {ext }}$ <br> $[\mathrm{C}]$ | $Q-1$ <br> $\left[\mathrm{~W} / \mathrm{m}^{2}\right]$ | $\Delta Q(2)$ <br> $\left[\mathrm{W} / \mathrm{m}^{2}\right]$ | $Q-2$ <br> $\left[\mathrm{~W} / \mathrm{m}^{2}\right]$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| I | 19 | 0 | 0.9 | 1.0 | 1.9 |
| 21 | 0 | 1.0 | 1.1 | 2.1 |  |
| 23 | 0 | 1.2 | 1.2 | 2.4 |  |
|  | 25 | -12 | 0.9 | 1.3 | 2.6 |

Figure 11 . Examples of heat flow caloulation (I: well insulated foundation, II: moderately insulated foundation) at different internal and external temperatures - floor not heatedo

The detached houses are built on adjacent sites of about 700-900 m². The earth consists mainly of diluvjal sand and some silt, and samples from test drililig have shown some variation as to the depth of the different strata However. all samples were rathex dryp having a water content of less than 12\%. The thermal conductivity of the earth acoording to [5] vaxies between 1.0 and $1.8 \mathrm{~W} / \mathrm{m}$. m (hexefore it was not attempted to make a single thermal model fit the five houses. Five different models were made based on temperam ture readings at different times of the year. As shown in Figure 12 the total heat resistance of the earth layers hardly varies in the five two-dimensional models and thus the results from the different houses may be compared directly The standard heat resistance values according to the Danish Rules [6] are included in Figure 12 . The thermal earth model for house $C$ has been used for all floor heating analyses.

| House | A | $\left.C^{*}\right)$ | $D$ | $E$ | $F$ |
| :--- | :---: | :---: | :---: | :---: | :---: |
| M(2-dim. model) | 4.0 | 4.0 | 4.0 | 4.0 | 4.1 |
| M(Danish Rules) | 1.5 | 1.5 | 1.5 | 1.5 | 2.5 |
| *) used for all floor heating analyses |  |  |  |  |  |

Figure 12. Heat resistance of earth layers. $M\left[\mathrm{~m}^{2} \mathrm{C} / \mathrm{W}\right]$.

DANISH STANDARD CALCULATION (ONE-DIMENSIONAL)

According to the Danish Rules [6] two different temperature differences are used for the calculation of the heat flow through slab-on-ground floors: the internal to external temperature difference (in our case 21 deg $C$ ) is used for a 1.0 m wide perimeter strip, and the internal to deep earth temperature difference (in our case 13 deg C) is used for the remaining floor area. similarly, different standard heat resistance values are used as indicated in figure 12. Vertical foundation insulation may be wholly or partially considexed as horizontal insulation of the perimeter strip depending on whether the vertical insulation reaches 1.0 m or less below the floor surface. It is obvious that alm though this method may yield satisfactory design heat losses it is unsuitable for the calculation of minimum surface temperatures. However, it may often be the only method available to the consultant engineer so the results have been included in this report fox comparison with the truex results from the two-dimensional calculations.

HEAT ELOWS AND MTNTMUM SURFACE TEMPERATURES
(EXISXING FLOORS, UNHEATED)

The traditional type of Eoundation for Danish slaboon-ground houses is a solid concrete structure cast on site, normally in an earth trench. In many houses the horizontal concrete slab and the foundation adjoin, but during the later years they are often separated by a thin strip of insulation, mostly 20 mm as shown to the right in figure 13. The floor indicated on the illustration is exactly like the floor of house $A$ described earlier and shown to the left in figure 13. The thermal earth model for house A has been used for the traditional Eoundation calculations. The results are listed in Figure 14.

The calculations for the commercially developed version of the house $A$ foundation shown in Figure 4 yield exactly the same results as for the prototype listed in figure 14 (A, 225 mm insulation). The main thermal advantage of the U-beam is the undiminished insulating efficiency at the Eootings.


Figure 13. Conservation house foundation (left) and traditional foundation (right).


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Q-1
    WMMQ Q-2
```

|  | Dani.sh | les | Two-dim | sional | del |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\begin{gathered} Q-D S \\ {\left[\mathrm{~W} / \mathrm{m}^{2}\right]} \end{gathered}$ | $\begin{gathered} t_{\min } \\ {[\operatorname{deg} \mathrm{C}]} \end{gathered}$ | $\begin{aligned} & \mathrm{Q}-1 \\ & {\left[\mathrm{~W} / \mathrm{m}^{2}\right]} \end{aligned}$ | $\begin{aligned} & \Delta Q(2) \\ & {\left[w / m^{2}\right]} \end{aligned}$ | $\begin{aligned} & \mathrm{Q}-2 \\ & {\left[\mathrm{w} / \mathrm{m}^{2}\right]} \end{aligned}$ | $\begin{aligned} & { }_{\mathrm{m} \min } \\ & {[\operatorname{deg} \mathrm{C}]} \end{aligned}$ |
| Traditional foundation | 2.7 | 20.5 | 1.5 | 3.3 | 4.8 | 18.5 |
| House A (225 mm insulation) | 2.1 | 20.5 | 1.5 | 0.9 | 2.4 | 20.2 |
| Do, at footing | 2.3 | 20.5 | 1.5 | 1.3 | 2.8 | 20.1 |
| House A ( 100 mm insulation) | 2.3 | 20.5 | 1.5 | 1.2 | 2.7 | 20.2 |
| Do, at footing | 2.5 | 20.5 | 1.5 | 1.4 | 2.9 | 20.2 |
| House C | 3.5 | 20.3 | 1.7 | 3.0 | 4.7 | 18.5 |
| House D | 2.5 | 20.6 | 1.6 | 1.0 | 2.6 | 19.6 |
| House E | 1.6 | 20.7 | 1.0 | 3.2 | 4.2 | 20.1 |
|  | 2.6 | 20.4 | 1.5 | 4.2 | 5.7 | 18.2 |
| House F ( $\mathrm{r} . \mathrm{f} .1 .1 .-2.4 \mathrm{~m}$ ) ${ }^{*}$ ) | 1.9 | 20.4 | 1.5 | 3.0 | 4.5 | 18.5 |
| $t_{\text {int }}=21.0 \mathrm{C} \quad t_{\text {ext }}=0.0 \mathrm{C} \quad t_{\text {ear }}=8.0 \mathrm{C}$ <br> *) prevailing |  |  |  |  |  |  |

Figure 14. Results of heat flow calculations.

The analyses of heated slab-on-ground floors were inspired by the floor construction of house $C$ figure 15, left. The floor insulation ( 50 man mineral wool and 250 mm expanded clay clinkers) must be considered insufficient in connection with a heated floor, at least for conservation houses. To the right in Figure 1530 mm external foundation insulation have been added to the construction as a possible retrofitting operation. Alternatively the effect of separating the floor slab from the foundation (as in figure 13, right) and replacing the concrete foundation top by expanded clay concrete is examined.

The floox construction recommended by several floor heating firms is shown in Figure 16 (left). The floor is insulated with 75 mm of expanded polystyrene and blocks of expanded clay concrete are used for the upper part of the foundation - the floor slab is separated from the foundation Calculaw tions have been made for the recommended insulation thickness as well as for an insulation thickness of 200 mm (Figm ure 16. right). In a slightly changed version of the recommended construction the separation has been omitted.

A construction that has been used in Denmark for some years for ordinary houses is shown to the left in figure 17. The foundation is built from solid blocks of expanded clay cone crete and is separated from the floor slab. In some countries with cold climates (eg Canada and finland) an external horizontal perimeter insulation is applied. Though it has not been practiced in Denmark we have inoluded the construction in the investigation in combination with the solid expanded clay concrete foundation, Figure 17 (right)。As the peximeter insulation cannot be accepted as surface material - fox aesthetic as well as for mechanical reasons the strip of polystyrene ( 100 mm thick and 1 or 2 m wide) is placed 50 mm below the ground surface.


Figure 15 . House $C$ foundation with/without external insum lation.


Figure 16. Foundation recommended by manueacturers of Eloor heating systems (left) and a version with improved floor insulation (right).


Figure 17. Solid expanded clay concrete foundation (left) and the same foundation with external horizontal perimeter insulation (right).

The insulated composite foundations at Hjortekær have given the inspiration to the final designs. Figure 18 shows a
 100 mm mineral wool in the floor. Calculations have been made for three different depths of the composite foundations $(y=0.60 / 0.70 / 1.50 \mathrm{~m})$ with and without separation of the floor slab.

Figure 19 (left) shows a sandwich foundation similar to the well insulated type in house $A$ (Figure 2), but having additional internal foundation insulation ( 50 mm mineral wool) and separation of the floor slab. Calculations have been made for slightly different versions of this foundation (with and without separation and/or the additional internal insulation) For the version without internal insulation the floor insulation has been increased to 200 mm (Figure 19, right). Finally insulation thicknesses of the com. posite foundation of 100 mm and 325 mm have been examined (no internal insulation and no separation).


Figure 18. Block built sandwich foundation with/without separation of eloor slab.


Figure 19. Precast sandwich foundation with/without internal insulation and improved floor insulation.

The different vexsions of the foundations included in the investigation are outlined in Figure 20 , and the results are listed in Figuxe 21 .


10


17
18


19


20


21


22


15


23

Figure 20. Outiines of foundations included in the invesm tigation.



Eigure 21. Results of floor heating analyses.

The external horizontal perimeter insulation mentioned earm liex is a possible retrofitting measure for older slabmonm ground houses. Eigure 22 shows a retrofitted construction with an original solid concrete foundation like in Figure 13, but in this case with 75 mm floor insulationo For the sake of argument floor heating is indicated. Fortum nately, in Denmark the combination is rare. The suggested retrofit may or may not include a 50 mm thick external vera tical insulation of the exposed part of the foundation (as shown to the right in Figure 22). The calculated heat flows are listed in Figure 23 。


Figure 22.
Two ways of retrofitting a solid concrete foundation (shown to the left) by applying external horizontal perimeter insulation with or without the external vertical insulation shown to the right。

| Version | Q-2 <br> (Floor <br> heated) <br> $\left[W / \mathrm{m}^{2}\right]$ | Q-2 <br> (Floor <br> not heated) <br> $\left[\mathrm{W} / \mathrm{m}^{2}\right]$ |
| :--- | :--- | :--- |
| Original foundation | 8.8 | 6.3 |
| Perimeter insulation 1.0 m wide | 8.5 | 6.1 |
| Do, with vertical insulation | 7.8 | 5.4 |
| Perimeter insulation 2.0 m wide | 8.4 | 5.8 |

Figure 23. Retrofit of concrete foundation, cf figure 22 。

## DISCUSSION

The comparison between the one-dimensional Danish standard calculations and the two-dimensional calculations (Q-DS and Q-2 of Figure 14) shows that the simplified calculation model underestimates the heat flow even though the heat resistance of the earth layers in the two models is $1.5 / 2.5$ and $4.0 \mathrm{~m}^{2} \mathrm{C} / \mathrm{W}$ respectively. The heat flow may be almost three times the values indicated by the Danish Rules.

All houses but $E$ have approx the same one-dimensional heat flow ( $Q-1$ ) through the floor - in house $E$ it is smaller (about two thirds of the average value). The resulting total heat flows ( $2-2$ ) show the extreme importance of an effective vertical perimeter insulation。

The composite foundations of house A and D are seen to be effective, the total heat flow being about half the reference heat flow for the traditional foundation. It should be noticed that the efficiency of the foundation of house A is only slightly reduced at the footings (insulation depth approx 0.50 m vs 1.0 m ) and similarly that the reduction of heat flow by a reduction of insulation thickness from 225 mm to 100 mm is small.

The internal vertical perimeter insulation of house $C$ is seen to be inefficient as the resulting heat flow equals that of the traditional foundation.


Figure 24. House E. Foundation, actual version and three (successively) improved versions.

Attention is called to the foundation construction of house E which serves as a warning example to house designers. It is a composite Eoundation insulated to the same depth as house $D$ and the floor is extremely well insulated, but due to the thick concreted floor slab being concreted to a concrete inner leaf the efforts are wasted - the heat flow is about as high as in a traditional foundation. The foundam tion and three suggested (successively introduced) improvements are illustrated in Figure 24 .

| Foundation | Illustrated | $Q-1$ <br> $\left[\mathrm{~W} / \mathrm{m}^{2}\right]$ | $\Delta Q(2)$ <br> $\left[\mathrm{W} / \mathrm{m}^{2}\right]$ | $Q-2$ <br> $\left[\mathrm{~W} / \mathrm{m}^{2}\right]$ |
| :--- | :--- | :--- | :--- | :--- |
| Traditional | Figure 13 | 1.5 | 3.3 | 4.8 |
| E Figure 24 a | 1.0 | 3.2 | 4.2 |  |
| E, improved | Figure 24 b | 1.0 | 2.9 | 3.9 |
| E, improved | Figure 24 c | 1.0 | 2.7 | 3.7 |
| E, improved | Figure 24 d | 1.0 | 1.4 | 2.4 |

Figure 25. House E. Effect of thermal bridge at inner leaf of foundation (Comparison to traditional foundation and some suggested improvements).

Firstly, the unusually thick concrete slab is replaced by an ordinary 100 mm slab $-\mathrm{second} y$, the floor slab is separated from the inner leaf of the foundation - and finally, the concreted inner leaf is replaced by blocks of expanded clay concrete. The corresponding heat flows are shown in Figm ure 25. The only truly efficient improvement is the replacement of the concreted inner leaf.

Exactly the same words of warning may be said about the basement foundation of house F. Figure 26 shows the actual construction and a modified version with a) separated floor
slab and b) only a slender block of concrete adjacent to the inner leaf of the wall and a block of expanded polystyrene adjacent to the wall insulation and outer leaf. The calculated heat flows are listed in Figure 27. The modification causes about a $40 \%$ reduction of the heat flows.


Figure 26. House F. Basement wall (foundation base). actual and improved version.

| Basement foundation |  | $\begin{gathered} 2-1 \\ {\left[\mathrm{~W} / \mathrm{m}^{2}\right]} \end{gathered}$ | $\begin{gathered} Q-2 \\ {\left[W / m^{2}\right]} \end{gathered}$ |
| :---: | :---: | :---: | :---: |
| r.f.l. - 1.2 m | F, actual <br> F, improved | $\begin{aligned} & 1.5 \\ & 1.5 \end{aligned}$ | $\begin{aligned} & 5.7 \\ & 3.6 \end{aligned}$ |
| r.f.l. - 2.4 m | F, actual <br> F, improved | $\begin{aligned} & 1.5 \\ & 1.5 \end{aligned}$ | $\begin{aligned} & 4.5 \\ & 2.8 \end{aligned}$ |

Figure 27. House F. Effect of thermal bridge at foundation base.

The results from Figure 14 are further supported by the results Erom Figure 21 （unheated floors）。 For unheated floors separation of the floor slab gives a heat flow reduc－ tion of 7－12\％。

The minimum internal surface temperatures reflect just about the same pattern．The $D$ value is lower than the $E$ value due to better wall insulation in house $E$ ．None of the tempera－ tures listed gives rise to alarm－the corresponding minimum temperature at a window with double glazing is approx 13 deg $C$ ．

A few general observations of the floor heating analyses are listed below：
－floor slab separation（20 mm）has almost no influ－ ence on the heat flows for heated floors．
－internal foundation insulation has very little effect on unheated floors，but may reduce the heat flow of heated floors by approx $10 \%$ ．
－external horizontal perimeter insulation is inef－ ficient for heated as well as for unheated floors．
－the analyses show that the heat flows through the floor constructions are 27－57\％highex when the floors are heated，averaging 50\％．The $27 \%$ apply to a floox construction with 200 mm horizontal insula－ tion and a sandwich foundation with 225 mm insula－ tion。
－for heated as well as for unheated floors the ear－ lier remarks about the effects of well insulated composite foundations and the insulation thickness and depth apply．Almost nothing is gained by increasing the insulation thickness from 225 to 325 mm or the depth from 600 to 1500 mm 。

- similarly, in a solid foundation the effect of having four blocks of expanded clay concrete instead of only the top two is hardly noticeable.
- it must be remembered that the marginal effect of adding insulation decreases with increased initial degree of insulation. This fact is emphasized by Figure 28 (as well as by Figure 21)。 The heat loss through an unheated floor insulated with 50 mm of mineral wool/cellular plastics is equal to the loss through a heated floor with 225 mm of insulation, but the heat loss through an unheated floor with 100 mm of insulation is equal to the loss through a heated floor with 325 mm of insulation.

|  | Q-2 <br> Floor insulation <br> $[\mathrm{mm}]$ | Q-2 <br> (Floor heated) <br> $\left[W / \mathrm{m}^{2}\right]$ |
| :---: | :---: | :---: |
| 50 | 4.8 | $\left[\mathrm{~W} / \mathrm{m}^{2}\right]$ |
| 100 | 4.0 | 3.1 |
| 150 | 3.6 | 2.7 |
| 200 | 3.2 | 2.5 |
| 250 | 3.0 | 2.2 |
| 300 | 2.8 | 2.0 |

Figure 28. Block built sandwich foundation. Calculated heat flows at different floor insulation thicknesses (mineral wool on top of 200 mm expanded clay clinkers)。

For slab-on-ground houses as well as for heated basements the application of insulated composite foundations must be recommended for heated as well as for unheated floors. The avoidance of thermal bridges, eg concretingr is extremely important. If the Eoundations have no cold bridges a simplified onemdimensional heat flow calculation model like the method prescribed in [6] may give acceptable results.

A slab-on-ground floor in a conservation house should not be heated, even as a lowmemperature system, but if so, the designer should increase the floor insulation to a minimum of 200 mm (mineral wool or cellular plastics) only to keep the heat loss at the same level as in a normal unheated floor construction, and the well insulated floor should be combined with a composite foundation insulated with approx 100 mm mineral wool or cellular plastics to a depth of approx 600 mm, Figure 29 。


Figure 29.
Foundation recommended by authors for energy conservam tion houses.

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